Tunneling through Weak Interactions: Comparison of Through-Space-, H-Bond-, and Through-Bond-Mediated Tunneling

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Results from ab initio electronic structure theory calculations on model systems allow for the detailed comparison of tunneling through covalently bonded contacts, hydrogen bonds, and van der Waals contacts. Considerable geometrical sensitivity as well as an exponential distance dependence of the tunneling is observed for tunneling through various nonbonded contacts. However, the fundamental result from the present study is that at most a modest difference is observed between tunneling mediated by H-bonds and tunneling mediated by van der Waals contacts at typical distances for each type of interaction. These results are considered in relation to the pathways model of Beratan and Onuchic, and implications for understanding long-range tunneling in biological systems are discussed.

1. Introduction

Electron-transfer reactions play an important role in a variety of biological processes. Understanding at a fundamental level of several features of biological electron transfers would be desirable in the design of synthetic systems that mimic their efficiencies and directionality. For example, the initial charge-transfer steps in photosynthetic electron transfer are quite rapid and yield considerably weaker decay with distance for electron or hole tunneling. Thus, when possible, tunneling should occur through bonded connections. However, when bonded connections represent a particularly circuitous route between the donor and acceptor, it is possible to tunnel through van der Waals contacts or, even, through interstitial waters. H-bond tunneling was parametrized as having a much weaker decay than van der Waals contacts (equivalent to two covalent bonds at a normal H-bond distance), whereas the through-space decay (i.e., van der Waals decay) was equivalent to decay through about nine covalent bonds at a normal methyl—methyl van der Waals contact distance. In part, the genius of this approach was the neglect of specific chemical details in the name of developing a general sense of distance dependence in biological electron transfers. It also had the distinct merit of allowing direct predictions for relative rates between different pathways in a protein. Beratan and Onuchic emphasized that their model is simplified—it neglects interference between pathways, treats all bonded connections as equivalent, and ignores orientation dependence except in an average sense. Nevertheless, it has helped set the parameters of the discussion of distance dependence in biological electron transfers for the past 20 years.

More detailed treatments of tunneling in model systems as well as actual systems of biological relevance have supported many of the ideas inherent in the pathways model. Quite detailed studies of tunneling in alkane chains have illuminated the nature of interference effects, but still validate the treatment of chemical units as leading to (nearly) equivalent decays with distance as the chain between donor and acceptor becomes elongated. A number of experimental studies have also investigated the impact of nonbonded contacts on the electronic coupling element and seen significant contributions to the coupling from weak interactions. For example, early studies by Beitz and Miller and more recent work by the Winkler and...
Gray group\textsuperscript{49,50} have shown that tunneling through solvent glasses (where nonbonded contacts must play a role) decays more rapidly than through-bond tunneling, but still presents a viable route for long-range electron transfer. In addition, a number of groups have developed synthetic model systems that allow for the examination of through-space and through-solvent tunneling. Zimm\textit{et al.} have explored tunneling mediated by solvent in their C-clamp molecules, where the through-bond tunneling pathway is sufficiently long that direct through-space tunneling between donor and acceptor becomes competitive\textsuperscript{51–54} Paddon-\textit{Row} and co-workers have synthesized analogous systems in which covalently attached pendant groups are interposed between donor and acceptor and significant effects on the coupling are observed.\textsuperscript{55}

Therien and co-workers have studied the effects of H-bonds on the coupling between a donor and acceptor and have found that the coupling through H-bonds is comparable to that through covalent bonds in their system, which is consistent with the pathways model.\textsuperscript{23} Winkler and Gray have also suggested that the H-bond network in aqueous sulfuric acid glasses may contribute to the higher-than-expected tunneling rates they observed in these systems.\textsuperscript{8}

A number of theoretical studies have also addressed how nonbonded contacts affect the electronic coupling between a donor and an acceptor. Newton studied tunneling through methanes and water molecules and found decay constants similar to those observed in straight-chain alkanes.\textsuperscript{56} His results also indicated that tunneling through H-bonds was competitive to through-bond tunneling in a set of model compounds. We have investigated tunneling through water using simple donors and acceptors and solvent configurations generated using molecular dynamics methods as well as model solvent geometries.\textsuperscript{57,58} The overall results were consistent with experimental results for tunneling through water, but somewhat surprising results were obtained using high-level ab initio wavefunctions to treat the model water geometries. There it was found that coupling through a water dimer was largely insensitive to the relative orientation of the waters. That is, H-bonded configurations provided no larger values of the coupling than some van der Waals contacts (having no conventional H-bonds). Furthermore, in comparisons of tunneling through van der Waals contacts and through-bond tunneling for straight-chain alkanes we found that through-space tunneling, although more rapidly decaying than through-bond tunneling, was not nearly as weak as one would expect on the basis of the pathways parametrization.

There is experimental precedent for somewhat surprisingly large through-space/van der Waals coupling.\textsuperscript{59} Tezcan \textit{et al.} examined interprotein/van der Waals coupling.\textsuperscript{59} Tezcan \textit{et al.} examined interprotein/van der Waals contact in crystals and found robust coupling despite the fact that the faces of the proteins along the line of centers between donor and acceptor presented largely non-H-bonded contacts through which to tunnel. In addition, in the studies of their C-clamp molecules, Zimm\textit{et al.} showed that intervening solvent could have marked effects on the coupling, further demonstrating that van der Waals contacts can play an integral role in mediating the coupling.\textsuperscript{54}

To the best of our knowledge, however, no theoretical studies have made direct comparisons of through-bond, H-bond, and through-space tunneling in systems where ab initio electronic structure techniques could be used to provide accurate assessments of the relative strengths of these couplings. Our goal in the present paper is to fill this gap and provide the theoretical results necessary to make these comparisons.

The results presented in the following sections will elucidate significant orientation effects in the tunneling through weak interactions. They will also show that the conclusions we draw are relatively insensitive to energetic effects. However, the fundamental result will be that, at least for the model systems treated here, there is no significant difference between tunneling through H-bonded or van der Waals contacts (at the inter-heavy-atom distances appropriate to each). We will further show that the strengths of tunneling through H-bond contacts and van der Waals contacts are intermediate between the pathways estimates for each of these types of contact.

It should be emphasized what we do not seek to accomplish at the outset. This is not an attempt to reparametrize the pathways model in the hopes of obtaining more accurate (but still coarse-grained) coupling elements from such a model. In the end, for treatments of biological systems it is now possible to use more detailed methods to probe the coupling element. Furthermore, it is not an attempt to somehow suggest that the pathways model was misguided because it treated tunneling via averaged parameters or because interference effects are neglected. It is, however, intended as a possible qualitative corrective. It is possible that the many successes of the model have led to the de facto adoption of the less tested aspect of the model, namely, that H-bonds mediate tunneling significantly better than other weak interactions. Although this may be the case in some systems, our calculations strongly argue that for the present model systems there is no significant difference between these two types of weak interactions.

The remainder of the paper is organized as follows. In section 2 we discuss the theoretical methods used and the model systems we treat. In section 3 we present our results for through-bond-, through-space-, and H-bond-mediated tunneling. In section 4 we discuss our results, and we present our conclusions in section 5.

2. Theoretical Methods

The systems treated here are of the form D–B–A, where D is the electron donor, A is the electron acceptor, and B is the bridge that may contain through-bond, van der Waals, or hydrogen-bond contacts. We exclusively consider tunneling in the +1 cation state of these systems, assuming a single electron transfer from D to A. The geometry of these structures, in most cases, was an idealized, model molecular geometry created in the GaussView environment.\textsuperscript{60} However, several systems possessing hydrogen-bond contacts were fully optimized using density functional theory\textsuperscript{61} with the B3LYP functional\textsuperscript{62} and the 6–31G\textsuperscript{*} basis.\textsuperscript{63–69} The idealized structures we consider are built under the assumption that all atoms follow VSEPR-like geometrical rules. The default bond lengths in the GaussView package were used for these idealized structures and are shown in Table 1 along with the values obtained in the optimizations associated with the hydrogen-bonded structures.

Four donor/acceptor groups were used with the majority of the calculations done using the –CH\textsubscript{2} radical for the donor/
acceptor group. Other donor/acceptor groups used in this study include the −SiH₂ radical, −NH₂, and −PH₂. For all of the systems presented, the donor group is always identical to the acceptor group (other than having a different number of electrons). The CH₂ and SiH₂ D/A groups had planar geometries, whereas the NH₂ and PH₂ D/A groups were trigonal pyramidal.

We consider two general types of systems, so-called “connected” and “disconnected” systems. The connected systems maintain a single all-trans covalent bonding network (all CH₂ units) between the donor and acceptor. The disconnected systems in idealized geometries are formed from the connected systems by deleting two central carbons (with their associated H atoms), yielding two subsystems having a total of n − 2 heavy atoms. Thus, each subunit maintains an all-trans structure. For investigation of tunneling through van der Waals contacts, we substitute the group of interest for heteroatom termination (to investigate H-bond contacts or dipole-dipole interactions) the decay constant for through-space decay (equation 2) does not hold, and it becomes necessary to use the generalized Mulliken–Hush method to calculate DA.

To compare our results with the pathways model, the DA values need to be converted into decay constants for through-bond, through-space, and H-bond contacts (ε₈, ε₆, and ε₄H, respectively). Following our previous results, the decay constant for a through-bond contact is calculated simply using the ratio of two DA values for two fully connected systems.

\[
\epsilon^2_C = \frac{H_{DA}^{+2}}{H_{DA}^0} 
\]

(3)

For the disconnected systems (either H-bond or van der Waals contacts) the decay constant for through-space decay (ε₈) or H-bond decay (ε₄H) is related to the ratio of the disconnected and the connected chain couplings via

\[
\epsilon_8(R) = \frac{H_{DA, disconnected, van der Waals}^{+3}}{H_{DA, connected}^0} \epsilon_C 
\]

(4)

\[
\epsilon_4H(R) = \frac{H_{DA, disconnected, H-bonded}^{+3}}{H_{DA, connected}^0} \epsilon_C 
\]

The above expressions can be understood on a qualitative basis in the following way. The transition from connected to disconnected systems in idealized geometries are formed from the connected systems by deleting two central carbons (with their associated H atoms), yielding two subsystems having a total of n − 2 heavy atoms. Thus, each subunit maintains an all-trans structure.
TABLE 2: \( H_{DA} \) (eV) Values Obtained Using Equation 1 for Connected Chain Carbon Donor/Acceptor Systems

<table>
<thead>
<tr>
<th>( n )</th>
<th>SA-MSCF/6-31G*</th>
<th>UHF/6-31G*</th>
<th>UCCSD/6-31G*</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>4.00E−01</td>
<td>5.11E−01</td>
<td>4.26E−01</td>
</tr>
<tr>
<td>6</td>
<td>2.19E−01</td>
<td>3.07E−01</td>
<td>2.60E−01</td>
</tr>
<tr>
<td>8</td>
<td>9.03E−02</td>
<td>1.47E−01</td>
<td>1.48E−01</td>
</tr>
<tr>
<td>10</td>
<td>3.13E−02</td>
<td>6.13E−02</td>
<td>7.44E−02</td>
</tr>
<tr>
<td>12</td>
<td>1.14E−02</td>
<td>2.66E−02</td>
<td>3.90E−02</td>
</tr>
</tbody>
</table>

Table 3: \( \epsilon_c \) Values Calculated Using Equation 2 for Connected Chain Donor/Acceptor Systems

<table>
<thead>
<tr>
<th>( n/2 )</th>
<th>SA-MSCF/6-31G*</th>
<th>UHF/6-31G*</th>
<th>UCCSD/6-31G*</th>
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<td>0.74</td>
<td>0.74</td>
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<tr>
<td>6/8</td>
<td>0.64</td>
<td>0.69</td>
<td>0.75</td>
</tr>
<tr>
<td>8/10</td>
<td>0.59</td>
<td>0.65</td>
<td>0.71</td>
</tr>
<tr>
<td>10/12</td>
<td>0.60</td>
<td>0.66</td>
<td>0.72</td>
</tr>
<tr>
<td>12/14</td>
<td>0.60</td>
<td>0.66</td>
<td>0.73</td>
</tr>
</tbody>
</table>

Using SA-MCSCF wavefunction and the \( \epsilon_C^{av} \) values appropriate to the SA-MCSCF connected chain from Table 3, we next considered disconnected chain results to calculate \( \epsilon_S(R) \), the through-space (or van der Waals) decay constant. Because our aim is to compare with the pathways model, we present results for \( \epsilon_S(R) \) directly rather than presenting \( H_{DA} \) values. In Table 4, we present the through-space decay constants for various donor/acceptor pairs, which were calculated using eq 4 (\( \epsilon_{C}^{av} \) for N, P, and Si as D/A were 0.69, 0.65, and 0.58, respectively). The calculations of \( H_{DA} \) used to construct Table 4 were performed using eq 2 because even though the chain was broken, \( C_{2h} \) symmetry was preserved as seen in Scheme 2. All of the donor/acceptors used show very similar exponential decay (\( \beta/2 \) values) and values for the decay constant at 3.4 Å. Because the transferring electron is localized on the donor or the acceptor, the electron-transfer process for these systems is expected to occur via McConnell-like superexchange. However, there seems to be little correlation between the energy gap between the donor/acceptor orbitals and bridge orbitals and the size of either \( \epsilon_C \) or \( \epsilon_S \). [Sample values for \( \Delta_{DB} \) in fully connected chains with a total of eight atoms are 2.6 eV for CH\(_2\) as donor, 2.85 eV for NH\(_2\), 3.5 eV for PH\(_2\), and 3.6 eV for SiH\(_2\) based on UHF (C and Si) or RHF (N and P) occupied orbital energy differences. We expect these values to vary somewhat depending on whether the chain length is changed or one considers disconnected systems.] The values of the coupling at 3.4 Å central C−C separation in Table 4 are expected to be somewhat higher than those for thermally accessible van der Waals contacts in this orientation. (MP2 calculations for two methanes oriented in the same way as the central methyl groups for this orientation show an energy rise of nearly 5 kcal/mol between 4 and 3.4 Å.) This is because the C−C line of centers connecting the central methyl carbons nearly coincides with a pair of C−H bonds. In this orientation one would generally expect a C−C distance closer to 4.2−4.4 Å on the basis of the C−H bond length and H atom van der Waals radius. At a central C−C distance of 4.2 Å in this orientation the coupling elements would be decreased relative to those at 3.4 Å by a factor of approximately 0.35. We thus decided to examine other van der Waals orientations that might allow closer approach of the central methyl groups.

Table 5 presents results from another methyl−methyl orientation. In this series of calculations we examine this structure as a function of the relative orientation of the fragments. For these calculations, the plane of one of the fragments was rotated relative to the other fragment, which we characterize by the dihedral angle between the two planes as seen in Scheme 3. During these calculations the distance between the two center methyls was frozen at 3.4 Å, which is the van der Waals distance for a head-on methyl−methyl contact. The donor/acceptor

SCHEME 2: Examples of Geometries Used in the Calculations Presented in Table 4
group used for any calculation should be assumed to be the CH$_2$ group unless otherwise noted. In Table 5, there is only a 25% change in the $\epsilon_S$ value from the largest value to the smallest value. It is perhaps surprising that the $H_{DA}$ value is not zero when the planes of donor and acceptor are perpendicular to each other. However, because the coupling between the donor/acceptor orbitals is mediated by the bridge framework, which is not linear, the local symmetry at the donor and acceptor need not determine the overall magnitude of the electronic coupling element.

In Table 6, a second orientation effect was examined by twisting either the donor or acceptor CH$_2$ group independently from the rest of the molecular subunit to which it belongs, shown in Scheme 4. Here we see a “zero” $H_{DA}$ value at 90° due to symmetry effects because a common symmetry plane occurs for both bridges at two points in the rotation. The trends seen in Table 6 are seen in the other donor/acceptor systems (results not shown).

Another degree of freedom is explored in Table 7 (see Scheme 5) in the dihedral angle between planes of the heavy atoms for each subunit, defining the angle of rotation. For these calculations, a 30° angular rotation should be equivalent to an $-30°$ angular rotation. This rotation examines how sensitive $\epsilon_S$ is to the nearest points of contact in the van der Waals interaction. From Table 7, it is evident that small angle changes do not greatly affect the size of the electronic coupling. However, when larger angles are attained, the decay constant $\epsilon_S$ decreases by more than a factor of 3.

In Table 8, various alcohol—alcohol contacts are examined to compare different hydrogen bond geometries and to directly compare hydrogen-bonded configurations to van der Waals contacts. In addition, we compare OH—OH H-bonds to two other H-bonded contacts (OH—NH$_2$ and OH—F) as well as several model van der Waals contacts. The first geometry (denoted model water dimer) was created from an optimized water dimer, appending the appropriate CH$_2$ bridge units, and the CH$_2$ donor/acceptor groups. The second geometry (OH—OH B3LYP opt) was created by optimizing the starting geometry seen in Scheme 6, with R = $-OH$, using the B3LYP/6-31G* method. In both cases two distinct O–O distances are tested, one being the optimized distance for each structure and the other having an O–O distance at 2.8 Å (for comparison with previous calculations). The third geometry is a model hydrogen bond system equivalent to the one seen is Scheme 6 with R = $-OH$ and the central O–O distance being 2.8 Å. The fourth geometry is a model van der Waals contact between two OH groups with the geometry being equivalent to the 180° dihedral rotation seen in Scheme 3, except that the terminal bridge units are alcohols instead of methyls and the central O–O distance is 2.8 Å. A fifth geometry is chosen to explore different van der Waals contacts and was created using the 0° dihedral rotation geometry seen in Scheme 3, except that one of the bridge terminus groups is an alcohol group and the central C–O distance is 3.2 Å. The final three structures are an alcohol—amine hydrogen bond, an alcohol—fluorine hydrogen bond, and an alcohol—methyl van der Waals contact. These final three structures were all optimized structures based on use of the B3LYP/6-311++G(d,p) method. The geometries from these optimizations are very similar to the alcohol—alcohol optimized structure, except slightly more linear. Several of these structures are depicted in Figure 1. In Table 8 it is seen that there is only a small difference between the $\epsilon_{H}$ values and the $\epsilon_S$ values, with the $\epsilon_S$ value being larger than some of the $\epsilon_{H}$ values.

One might imagine that tunneling through H-bonds, which are inherently less symmetrical than methyl—methyl van der Waals contacts, might be significantly more sensitive to the relative D/A orientations. To test this we used the OH—OH B3LYP optimized structure from Table 8 with the O–O distance set equal to 2.8 Å and then rotated the donor or acceptor in 30° increments from 0° to 180°. The angle corresponding to the maximum coupling for each individual rotation was then taken to construct a dimer with (approximate) D and A orientations leading to maximal coupling. This approximate maximal coupling orientation yields a value of $H_{DA}$ (and thus $\epsilon_S$) approximately 1.7 times that of the value in Table 8 ($\epsilon_{H}$ near 0.097 rather than 0.055 as in Table 8). We performed the analogous rotation of D and A for a geometry related to this same optimized H-bond geometry, except that the two fragments were rotated relative to each other about the O–O line of centers by 180°. Here the value of $\epsilon_{H}$ was 0.10 before optimization of the D/A orientations and 0.19 after optimization. Thus, although such angle variations could lead to somewhat larger values of the decay constants, we would not expect drastic changes were such angle variations to be pursued in general.

In Table 9 three distinct planar hydrogen bond structures (geometries shown in Scheme 6) were examined and parameterized so that the values can be compared to the previous van der Waals results and to the results of the pathways model (CH$_3$ donor and acceptor). The reference distance between terminal atoms in the disconnected structure was chosen to be 2.8 Å to represent a normal hydrogen bond length. These results show that the $\alpha/\epsilon_{H}$(2.8 Å) values for the various contacts are fairly similar and are also similar to previously calculated $\epsilon_S$ values. One notable difference among these contacts is the fact that...
the $\beta/2$ value for the fluorine system is larger than that for the other two systems. This could result from the fact that fluorine is very electronegative, which will cause the electron density to be locally compact, leading to a greater sensitivity to the separation distance. Whereas at large separation the decay with distance of $H_{DA}$ will be controlled by the energy of the donor and acceptor, the local structure of the electron density clearly also plays a role for small variations in distance.

Table 10 demonstrates the differences in $\epsilon_H$ values based on the choice of donor/acceptor groups. For all of these systems, an alcohol–alcohol hydrogen bond system at 2.8 Å was used as the reference distance and the orientation was the same as that of Scheme 6. There is modest sensitivity to the D/A choice, on a scale comparable to the sensitivity found for van der Waals contacts (Table 4).

In Table 11, the effects of increasing the size of the basis set on two disconnected chain geometries are examined. The first geometry is similar to the OH–OH hydrogen bond from Table 8 based on the model water dimer geometry presented there, but rotated around the O–O line of centers (yielding a somewhat greater coupling element than that quoted for the model water dimer structure). The second geometry is the van der Waals structure at the 120° angle of Table 5. The previous results for these geometries using the 6-31G* basis are presented again in Table 11, along with results from systematic expansion of the basis up to the 6-311+G(d,p) basis set. Because all of the results presented are within about 15% of the 6-31G* results, we believe that the 6-31G* basis was sufficiently accurate for our purposes.

Using a variety of systems, Table 12 examines the effect on the electronic coupling of including correlation via the EOM-CCSD method. The variation in the coupling between correlated and uncorrelated results is at most 25%. Results for other geometries (not shown) tell a similar story—a maximum change in the coupling of about 33%. Thus, the uncorrelated SA-MCSCF method appears to be sufficiently accurate for the electronic coupling of including correlation via the EOM-CCSD method. The variation in the coupling between correlated and uncorrelated results is at most 25%. Results for other geometries (not shown) tell a similar story—a maximum change in the coupling of about 33%.

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We also applied FOCI and SOCI wavefunctions to model CH$_3$–CH$_3$ van der Waals geometries. The largest variation in the coupling compared to the SA-MCSCF results was a factor of 1.5. We again concluded that correlation had at most a quantitative effect on the coupling and that the conclusions we draw would not be altered by the inclusion of correlation.

4. Discussion

The pathways model has been used extensively as a conceptual and computational point of reference for understanding biological electron transfers. From a conceptual point of view its main elements are that (i) through-bond coupling decays slowly, (ii) tunneling through weak interactions decays quite rapidly, and (iii) H-bonds, although they are relatively weak interactions, still mediate the electronic coupling quite effectively. For comparison with our calculated results we note the pathways model values for $\epsilon_C = 0.6$, $\epsilon_S(3.4 \text{ Å}) = 0.010$, and $\epsilon_H(2.8 \text{ Å}) = 0.36$ (the two distances being the van der Waals distances for head-on contact for methyl groups and a conventional H-bond length, respectively).

In a general sense, our results support the pathways model. The through-bond decay constant for the connected alkane chains is quite similar to that of the pathways model, is weakly dependent on the donor or acceptor, and is considerably larger than the decay constant for tunneling through weak interactions. Clearly the through-bond coupling will vary with geometry, and our results are focused solely on all-trans geometries. However, the variation is not expected to qualitatively alter these conclusions. Our results support the notion that electrons or holes should tunnel through-bond whenever the path connecting D and A is not too circuitous.

We find considerable variation in the decay constants for H-bond and van der Waals contacts as a function of geometry, making it difficult to be absolutely general about the relative strengths of the two types of interactions. We observe, for the range of geometries considered here, that decay constants for either type of interaction are generally below 0.1 (for the reference distances considered) but above 0.03. Considering only the largest interactions of each type, we obtained an H-bond decay constant of nearly 0.2, with a thermally accessible van der Waals decay constant of at most 0.085. This would argue that the H-bonded contacts have the potential to produce couplings larger than the van der Waals contacts. However, taken in aggregate our results indicate that, if there are differences on average between the two types of weak-coupling-mediated tunneling, they are modest at best. Recent work by Prytkova, Kurnikov, and Beratan has also posited a somewhat greater size for through-space coupling than in the original pathways model. Their results suggest better agreement for the pathways model with ab initio data when they decrease the through-space decay constant from 1.7 to 1.0 Å$^{-1}$. In their case the decreased decay constant size was in part accounted for by the assumption of tunneling at elevated energies via excited states. In the present cases we are considering tunneling for low-energy electrons and still find larger than expected through-space tunneling.

Of course, the question of the relative size of the through-bond and through-space/H-bond coupling is in part dependent on how one calculates the through-space coupling, and there is some ambiguity associated with the optimal method for doing this. For example, consider the value of $\epsilon_S$ (derived from Table 4) for symmetrical van der Waals contacts at 3.4 Å for D/A = CH$_2$, 0.145. The value of $\epsilon_C$ used to obtain this (and all values of $\epsilon_S$ and $\epsilon_H$ in the rest of the paper) was the average value from Table 3, that is, $\epsilon_C = 0.64$. One might have imagined that a better choice would have been that appropriate to the $n = 10$ (connected chain) result, $\epsilon_C = 0.588$, because the connected...
Using eq 5 we find that $\epsilon_S(3.4\,\text{Å}) = 0.036$, a significant difference compared to the previous two estimates. To assess the validity of this result, we performed calculations based on the $n = 12$ and $n = 14$ connected and disconnected chains. If variation in $\epsilon_C$ is an issue (necessitating use of eq 5), then $\epsilon_S$ should vary significantly when eq 5 is used to calculate $\epsilon_S$ on the basis of the $n = 12$ and $n = 14$ systems. As Table 13 demonstrates, the $\epsilon_S(3.4\,\text{Å})$ value based on the $n = 10$ system is actually lower than the $\epsilon_S(3.4\,\text{Å})$ value for either the $n = 12$ or $14$ system. Thus, we expect that at worst our $\epsilon_S$ values underestimate what we would obtain for longer systems and that the conclusions drawn here about the relative sizes of these interactions should be relatively robust. Furthermore, because the same analysis is used to compute $\epsilon_C$ and $\epsilon_S$, these two quantities can be directly compared, independent of how one might prefer to derive either one by itself.

A second issue to consider in comparing coupling through H-bonds and van der Waals contacts is the distance between heavy atoms in the van der Waals contact. In the present study our H-bond reference distances are near 2.8 Å, and we have chosen a reference value of 3.4 Å for methyl–methyl van der Waals contact. This value for methyl–methyl van der Waals contacts allows direct comparison with previous calculations and is in agreement with the expected C–C distance for head-on approach of two methyl groups. However, whereas H-bonds have generally well-defined lengths, van der Waals contacts range over considerable lengths and will often depend on how a protein folds. Their lengths will also likely be more susceptible to thermal fluctuations than H-bonds. Methyl–methyl van der Waals contacts have been observed in the range of 3.4–4.2 Å in crystal structures of organic molecules. In a crystal structure of cytochrome $c$ a C–C distance of 3.22 Å is found between an isoleucine and leucine (residues 85 and 94), but there are certainly larger van der Waals contact distances observed as well. An increase in distance from 3.4 to 4.0 Å would decrease our $\epsilon_S$ values by approximately a factor of 2 (on the basis of the exponential distance dependence presented in Table 3), which is still a considerably larger coupling than the factor of 36 decrease for through-space coupling relative to H-bonds in the pathways model. Thus, if one compared “normal” length H-bonds to stretched van der Waals contacts, coupling through H-bonds would be, on average, about a factor of 2 larger. However, if one compares tunneling through each type of contact at near-optimal lengths for the interaction, the tunneling decay parameters are relatively similar. Finally, we note that if we were to compare the two types of contacts at a single fixed distance (e.g., 2.8 Å), we expect that tunneling through van der Waals contacts would be at least as efficient as tunneling through H-bonds, because the methyl groups would be quite close and in a relatively high potential energy configuration. This is, however, a relatively unlikely geometry for van der Waals contacts, and we have not considered it here.

and disconnected systems used to derive the results of Table 3 were based on $n = 10$ systems. In this case, $\epsilon_S(3.4\,\text{Å}) = 0.112$ (based on the connected $H_{DA}$ value of 0.0313 eV for the $n = 10$ case and the disconnected $H_{DA}$ value of 0.0173 eV). A third, distinct method for calculating $\epsilon_S$ would be to use $\epsilon_C = 0.74$ (for the $n = 4/6$) for the disconnected chain (because there are two distinct $n = 4$ chains in the $n = 10$ disconnected chain results), whereas for the connected $n = 10$ chain $\epsilon_C = 0.588$ would be used (see eq 5).

$$\frac{H_{\text{DA}}^{\text{disconnected},n=10}}{H_{\text{DA}}^{\text{connected},n=10}} = \frac{\epsilon_S^{n=10/12,8}}{\epsilon_S^{n=46,5}} = \epsilon_S(3.4\,\text{Å}) \quad (5)$$

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TABLE 8: Comparison of Various Alcohol—Alcohol and Hydrogen Bond Contacts

<table>
<thead>
<tr>
<th>structure</th>
<th>contact</th>
<th>$H_{DA}$ (eV)</th>
<th>$\epsilon_H$ or $\epsilon_S$</th>
<th>distance between heavy atoms (Å)</th>
</tr>
</thead>
<tbody>
<tr>
<td>water dimer</td>
<td>H-bond</td>
<td>0.00244</td>
<td>0.020</td>
<td>2.8</td>
</tr>
<tr>
<td>model water dimer</td>
<td>H-bond</td>
<td>0.00223</td>
<td>0.019</td>
<td>2.91</td>
</tr>
<tr>
<td>OH-OH/B3LYP opt</td>
<td>H-bond</td>
<td>0.00673</td>
<td>0.055</td>
<td>2.8</td>
</tr>
<tr>
<td>OH-OH/B3LYP opt</td>
<td>H-bond</td>
<td>0.00649</td>
<td>0.054</td>
<td>2.85</td>
</tr>
<tr>
<td>model H-bond</td>
<td>H-bond</td>
<td>0.0117</td>
<td>0.098</td>
<td>2.8</td>
</tr>
<tr>
<td>OH-OH VDW contact</td>
<td>VDW</td>
<td>0.00847</td>
<td>0.071</td>
<td>2.8</td>
</tr>
<tr>
<td>model VDW OH−CH$_3$</td>
<td>VDW</td>
<td>0.00710</td>
<td>0.059</td>
<td>3.2</td>
</tr>
<tr>
<td>opt OH−NH$_3$</td>
<td>VDW</td>
<td>0.00633</td>
<td>0.053</td>
<td>2.90</td>
</tr>
<tr>
<td>opt OH−F</td>
<td>H-bond</td>
<td>0.00599</td>
<td>0.050</td>
<td>2.91</td>
</tr>
<tr>
<td>opt OH−CH$_3$</td>
<td>VDW</td>
<td>0.00153</td>
<td>0.013</td>
<td>3.1</td>
</tr>
</tbody>
</table>

Contact indicates the qualitative character of the interaction between the two central units on the pair of disconnected chains. The origin of the specific geometries is outlined in the text. The final column indicates the distance between the pair of central heavy atoms.
As suggested in the analysis that led to the pathways model, we find considerable orientation dependence in the coupling through the weak interactions considered here. The couplings via different van der Waals orientations examined in Tables 5–7 show significant variation with geometry, and it is clear from the consideration of H-bonds that small geometry changes can lead to large changes in the coupling. The pathways model treats these orientation effects in an average sense, and they are indeed non-negligible.

One might ask how sensitive the present results are to D/A energy variations. The energies of the transferring electron relative to the bridge HOMO vary over a range of about 2.5–4 eV in the present examples. For photoexcited electron transfer one would expect a larger D/A bridge gap and a smaller D/A IP. The present results cannot directly comment on these larger gap situations; however, past results for tunneling through water, for both H-bonded and non-H-bonded configurations, suggest relatively modest variations in the coupling at close contact for significantly larger changes in D/A bridge energies.57,58 We expect similar behavior for these systems, and this is consistent with the relatively weak dependence of tunneling through bond on D/A energy when the D/A energies are well-separated from the bridge band edges.90 Nonetheless, we still expect the D/A energy to affect the exponential decay constant for the coupling at large distances. In addition, it is interesting to note that the decay with distance is affected (locally) by the nature of the central contacts, with H-bond-mediated tunneling through F decaying more rapidly with distance than tunneling through methyl groups. At large distances this decay should depend largely on the D/A energy, but it is clear that at shorter distances the decay depends to some extent on the features of the local electron density.

The central, and somewhat surprising, result of the present work is the similarity between the coupling through-space (van der Waals contacts) and that through H-bonds. As noted above, the pathways model (on the basis of a pair of simple analytical models) suggested that the difference in the size of these couplings should be a factor of about 36 (at distances of 3.4 and 2.8 Å for through-space- and H-bond-mediated coupling, respectively). Despite the relatively large orientation dependence observed in our results, we find H-bond-mediated coupling to be a good deal weaker and through-space coupling to be a good deal stronger than these predictions. In some sense this should not be too surprising, because we are comparing tunneling efficiencies through two weak interactions and there is little reason to assume that the efficiency of tunneling should necessarily scale with the strength of interactions at these low energies.

It is possible that this result is specific to the systems studied here. However, the robust nature of the result with respect to D/A energy and orientation suggests that it may be relatively general. One might also suggest that the basis and SA-MCSCF treatment used here are inadequate for uncovering the difference between the two types of tunneling, but our extended basis set and correlation results (as seen in Tables 11 and 12) do not show dramatic changes in the coupling.

If these results are general, they suggest that for fixed geometries there are really only two types of coupling—bond-mediated and weak-interaction-mediated, with bond-mediated coupling being at least 6 times slower decaying (i.e., one weak-interaction tunneling event is equivalent to tunneling through at least four covalent bonds, and often more like five or six covalent bonds). If that is true, what might account for previous suggestions that H-bonds are significantly more effective at mediating coupling than are van der Waals contacts?23–29

One possibility is that the comparisons between H-bonded and covalently mediated couplings have been made for covalent structures that possess interference effects and/or poor coupling to the donor or acceptor due to steric effects.23 Subtle geometry changes not accounted for by counting bonds may play a role that could mask weaker coupling by H-bonds. We are pursuing calculations to test this, but the present results do not support suggestions of particularly robust coupling through single H-bonds.

It is also possible that H-bonds might be found to be more effective at mediating coupling than van der Waals contacts than our results indicate due to a secondary effect. That is, the strengths of the couplings through van der Waals and H-bonds might be quite similar, but the H-bond’s strength might confer extra stability to the overall structure with respect to geometrical fluctuations. It is well-known now that small fluctuations can yield rapid and often dramatic changes in the coupling.57–95 It is possible that the reason H-bonds may be better contacts, if indeed they are, is due to the extra stability of the structure when H-bonds are present rather than absent, giving rise to smaller coupling fluctuations and (if the geometry near the minimum corresponds to relatively large coupling) an overall rate enhancement.

Figure 1. Subset of the structures considered in the calculations presented in Table 8.
Of course, to investigate detailed questions concerning the electronic coupling in systems of biological interest, one will need to go beyond coarse-grained models of the pathways type to probe subtle, specific coupling enhancements with changes in local structure. These calculations have been pursued in a number of groups with great success.\(^{34,36,42,96–102}\) We have recently implemented a one-electron version of the generalized Mulliken–Hush approach\(^{103,104}\) (Koopmans’ theorem GMH, along with a density functional theory-based variant, Kohn–Sham GMH/KS-GMH) that will allow us to calculate couplings in systems of the appropriate scale for biological electron transfers. Thus, we are not advocating that with improved parameters one could eschew detailed calculations and obtain accurate results.

Rather, we are arguing that in thinking about the paths through which electrons might tunnel in biological (or synthetic) electron-transfer systems, it may be important to reconsider the roles of both through-space and H-bond tunneling. In particular, for close van der Waals contacts tunneling may be equally effective as that through H-bonds, and a good deal larger than has been previously supposed. In addition, when considering tunneling through particular H-bonds, it may in fact be the case that the intrinsic tunneling is not significantly larger than that through other weak interactions and that the overall net tunneling comes about through the participation of a broader array of contributions from many weak interactions. Whatever the case, the present study suggests that a new consideration of weak interactions in biological electron transfers be undertaken, using detailed, many-electron approaches, and specific focus be given to tunneling through weak interactions. The tunneling current approach of Stuchebrukhov\(^2,3,105\) and co-workers appears to be ideally suited to address this question in realistic systems.

5. Conclusions

We presented results from ab initio electronic structure theory calculations on model systems that allow detailed comparisons of tunneling through bonded contacts, H-bonds, and van der Waals contacts. Considerable geometrical sensitivity as well as an exponential distance dependence of the tunneling is observed for tunneling through nonbonded contacts. However, the fundamental result from the present study is that we find at best modest differences between tunneling mediated by H-bonds and tunneling mediated by van der Waals contacts at conventional distances for each interaction. We suggest that this may imply that van der Waals contacts may be more important in biological electron transfers than has been previously assumed and that the focus on specific H-bonds that mediate interchain tunneling may exaggerate their importance. However, we also discuss a possible secondary role H-bonds may play in controlling geometrical fluctuations that can give rise to increased tunneling.

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References and Notes